

#### UNIFIED SOLVER STRATEGY FOR FLOATING-POINT Jaideep Ramachandran, Northeastern University jaideep@ccs.neu.edu

# GOAL

To come up with a strategy for solving Floating-Point Arithmetic formulas that takes into account:

- Nature of input formulas (e.g., complexity)
- Applicability of abstractions

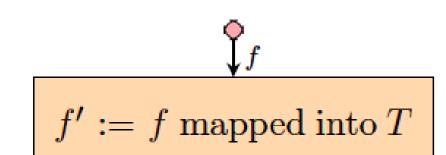
\* Performance of "proxy theories"

### EXAMPLES

- Linear with arithmetic operations reordered  $|(x + (y + z)) - ((x + y) + z)| > \epsilon$
- Non-linear  $10.25 \le x^2 + y^2 \le 10.5$
- Non-linear with arithmetic operations reordered  $|(x+y)^2 - ((x^2 + (2*x)*y) + y^2)| > \epsilon$

May need different strategies to solve!

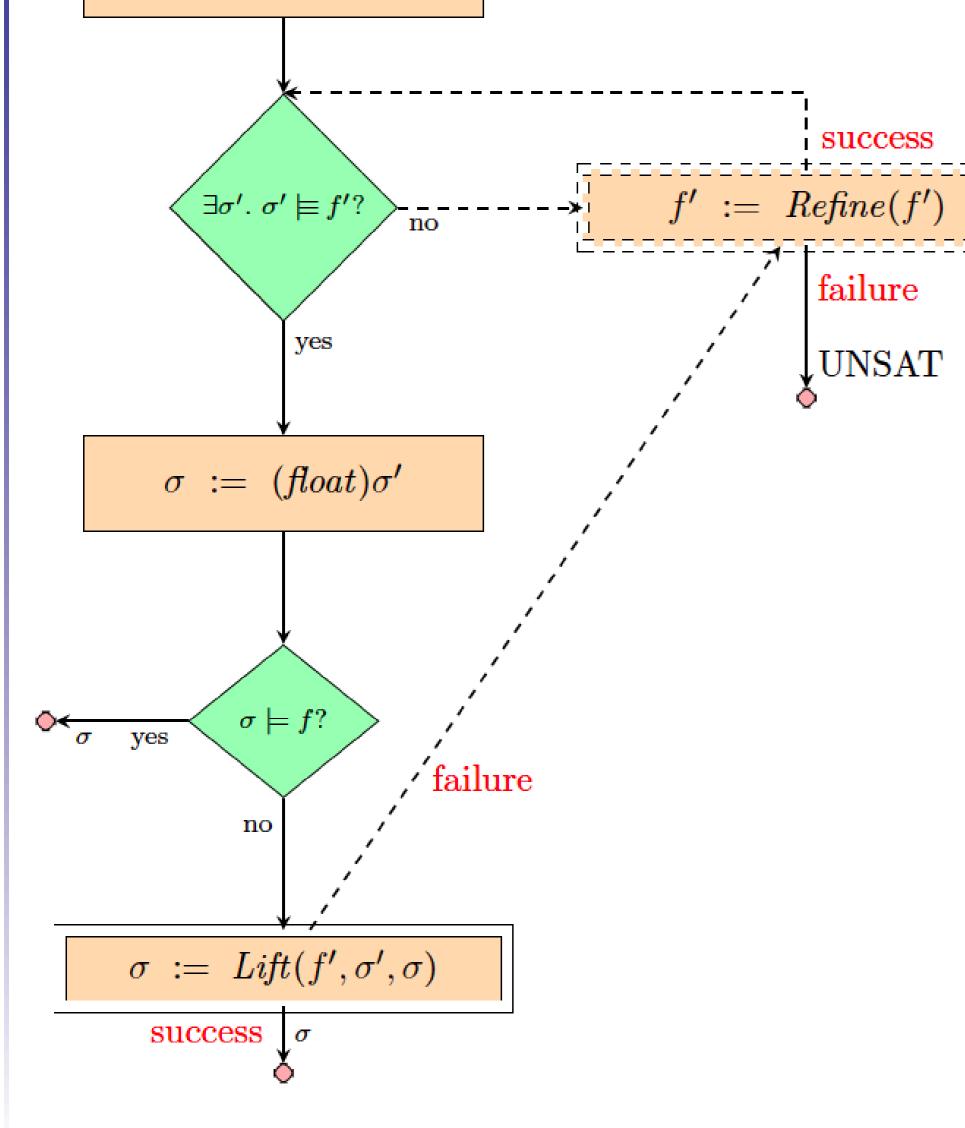
## MODEL LIFTING ARCHITECTURE



# SOLUTION: UNIFIED STRATEGY

**Require:** *f*: FPA formula

- 1: if Linear(f) then



- return MOLLY<sup>MRFPA</sup>(f) // mixed real-2: float reasoning
- 3:  $result := MOLLY^{RA}(f) // pure real abstraction$
- 4: if  $result \neq failed$  then
- return result 5:
- 6:  $result := MOLLY^{dREAL}(f) // numerical solving$
- 7: if  $result \neq failed$  then
- return result 8:
- 9: return MOLLY<sup>RPFPA</sup> // reduced precision

#### MOLLY CONFIGURATIONS

Name Spec	Molly <sup>RA</sup>	Lazy Realizer	Molly <sup>MRFPA</sup>	Molly <sup>dReal</sup>	Molly <sup>RPFPA</sup>	Approx
Proxy theory	RA	RA	RA	Reals + $\delta$ -sat	RPFPA	RPFPA
Proxy solver	Z3	Realizer++	Realizer++	dReal	Mathsat	MATHSAT
Lifting?	$\checkmark$	×	$\checkmark$	$\checkmark$	$\checkmark$	×
Refinement?	×	$\checkmark$	$\checkmark$	×	$\checkmark$	$\checkmark$
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Experimental evaluation indicates there is no clear winning configuration across all formulas. Hence the need for a unified strategy.